

AP Physics - Momentum - Conservation of Momentum

Note Title

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So far you know about two of the four conservation laws of the universe: conservation of mass, and conservation of energy. Today, you will learn a third: Conservation of Momentum

Conservation of Momentum - In the absence of an external force, the total momentum of a system will remain constant.

$$\Sigma \vec{P}_{\text{before}} = \Sigma \vec{P}_{\text{during}} = \Sigma \vec{P}_{\text{after}}$$

In one dimension with two objects (m_1 and m_2) this becomes:

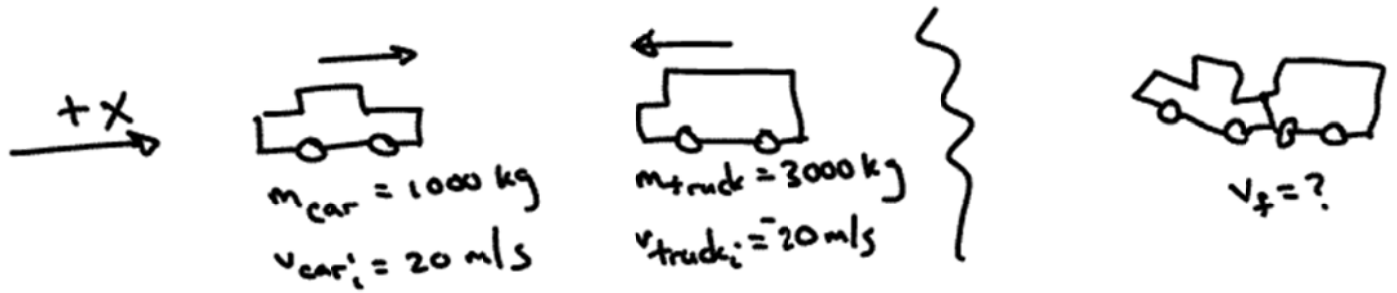
$$m_1 \vec{v}_{1i} + m_2 \vec{v}_{2i} = m_1 \vec{v}_{1f} + m_2 \vec{v}_{2f}$$

Example: Billiard balls of mass m . One at rest, another with an initial velocity v_i . Assuming that after the collision, the first ball stops, what is the velocity of the second ball after the collision?

Before	{	After	
$\begin{array}{c} \text{O} \rightarrow \\ m \\ v_{1i} = v \end{array}$		$\begin{array}{c} \text{O} \\ m \\ v_{1f} = 0 \end{array}$	$\begin{array}{c} \text{O} \rightarrow \\ m \\ v_{2f} = ? \end{array}$
$\begin{array}{c} \text{O} \\ m \\ v_{2i} = 0 \end{array}$		$= m(0) + m v_{2f}$	
$mv + m(0)$		$= m(0) + m v_{2f}$	
$mv = m v_{2f}$			
$v_{2f} = v$			

\therefore The second ball leaves with the same velocity that the first ball enters!

Example: A 1000 kg car crashes into and sticks to a 3000 kg truck. The car's initial velocity is 20 m/s to the right. The truck's initial velocity is 20 m/s to the left. What is the final velocity of the combined mass?



$$m_{\text{car}}v_{\text{car},i} + m_{\text{truck}}v_{\text{truck},i} = (m_{\text{car}} + m_{\text{truck}})v_f$$

$$v_f = \frac{m_{\text{car}}v_{\text{car},i} + m_{\text{truck}}v_{\text{truck},i}}{m_{\text{car}} + m_{\text{truck}}}$$

* Don't forget the negative velocity of the truck!!!

$$\rightarrow v_f = \frac{(1000)(20) + (3000)(-20)}{1000 + 3000}$$

$$v_f = -10 \text{ m/s}$$

\therefore The combined mass travels at 10 m/s to the left (the truck wins)